

# Forecasting Chronic Diseases using Data Fusion

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**Joint work with**

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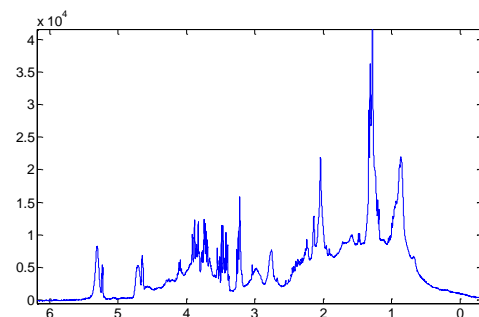


# Motivation: Joint analysis of measurements from multiple platforms has the potential to enhance biomarker discovery!

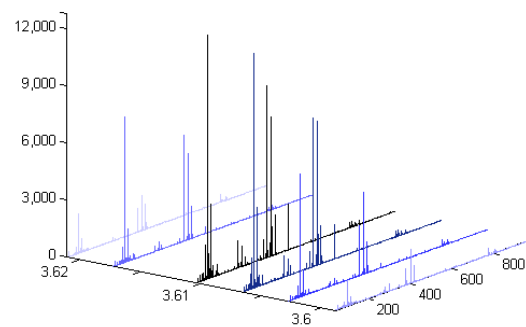
**Metabolomics:** The goal is to detect a wide range of chemical substances in biological fluids, e.g., blood, and to identify the chemicals related to certain conditions such as food intake and various diseases, e.g., cancer.



Possible to measure  
using different  
analytical methods



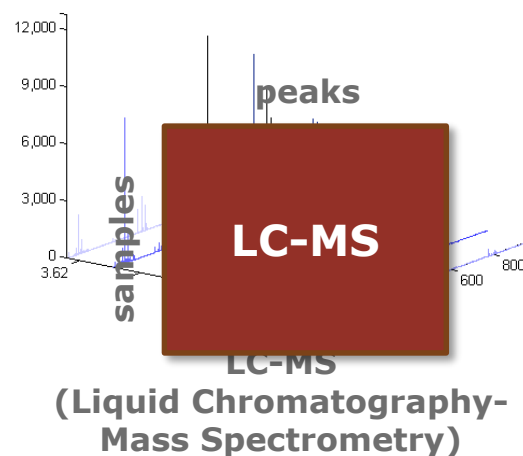
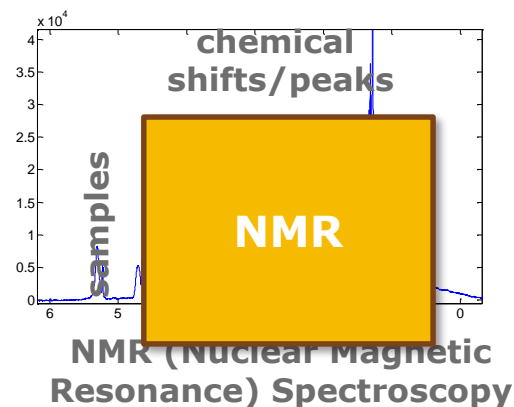
**NMR (Nuclear Magnetic Resonance) Spectroscopy**



**LC-MS  
(Liquid Chromatography-  
Mass Spectrometry)**

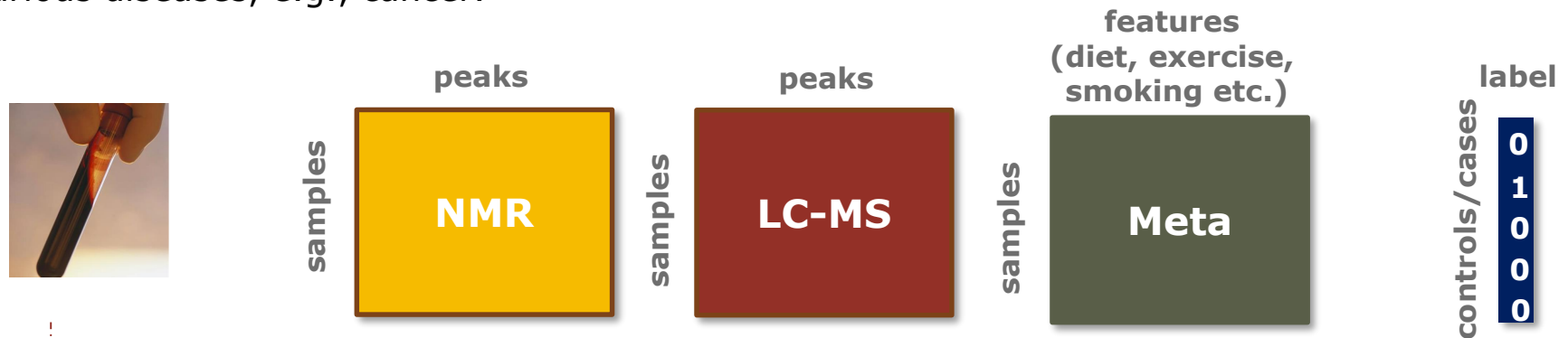
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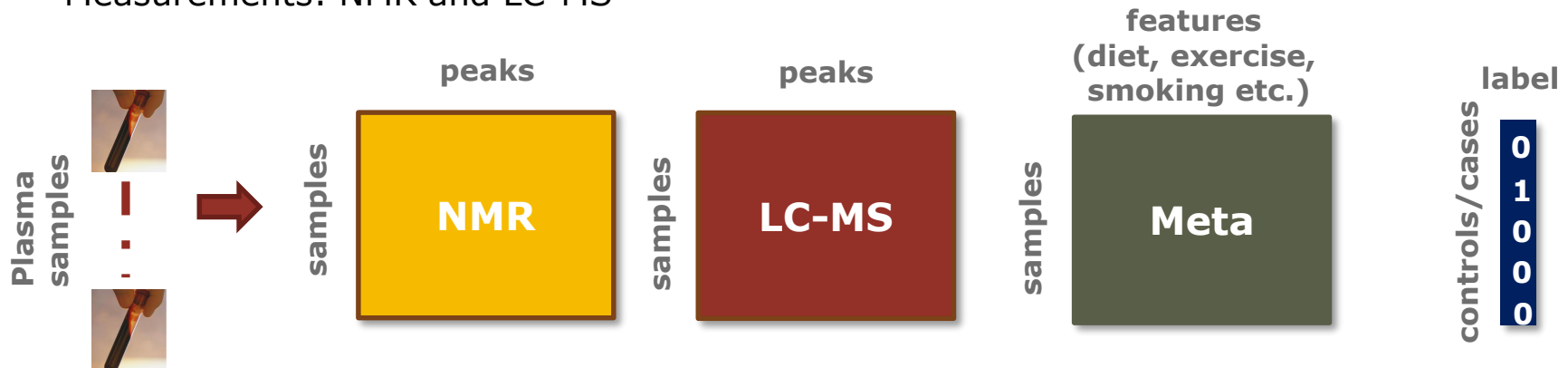
**Metabolomics:** The goal is to detect a wide range of chemical substances in biological fluids, e.g., blood, and to identify the chemicals related to certain conditions such as food intake and various diseases, e.g., cancer.



- 1. Given these data sets, can we forecast whether people will have certain diseases in near future?*
- 2. Does data fusion improve our forecasting performance?*
- 3. Can we capture biomarkers? Are we confident with those biomarkers?*

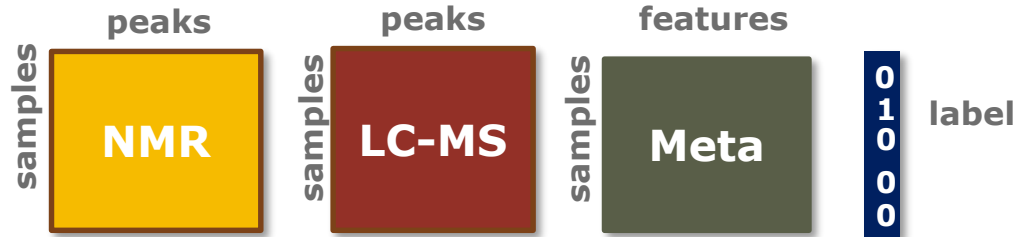
# Our Data: Samples from subjects enrolled in the Danish Diet, Cancer and Health (DCH) Cohort [Tjønneland et al., 2007]

- Plasma samples (non-fasting) from subjects free of cancer at the time of sample collection (1993-1997). Some of those subjects develop the disease over time (time span is approximately up to 10 years).
- We are, in particular, interested in Acute Coronary Syndrome, Breast Cancer and Colorectal Cancer.
- Measurements: NMR and LC-MS



1. **Given these data sets, can we *forecast* whether subjects will develop the following diseases?**
  - **Acute Coronary Syndrome (ACS)**
  - **Breast Cancer**
  - **Colorectal Cancer**
2. **Does data fusion improve our forecasting performance?**
3. **Can we capture biomarkers? Are we confident with those biomarkers?**
  - **We will look into smoking and coffee to validate our approach.**

# Supervised Data Fusion (a.k.a. multi-view learning)

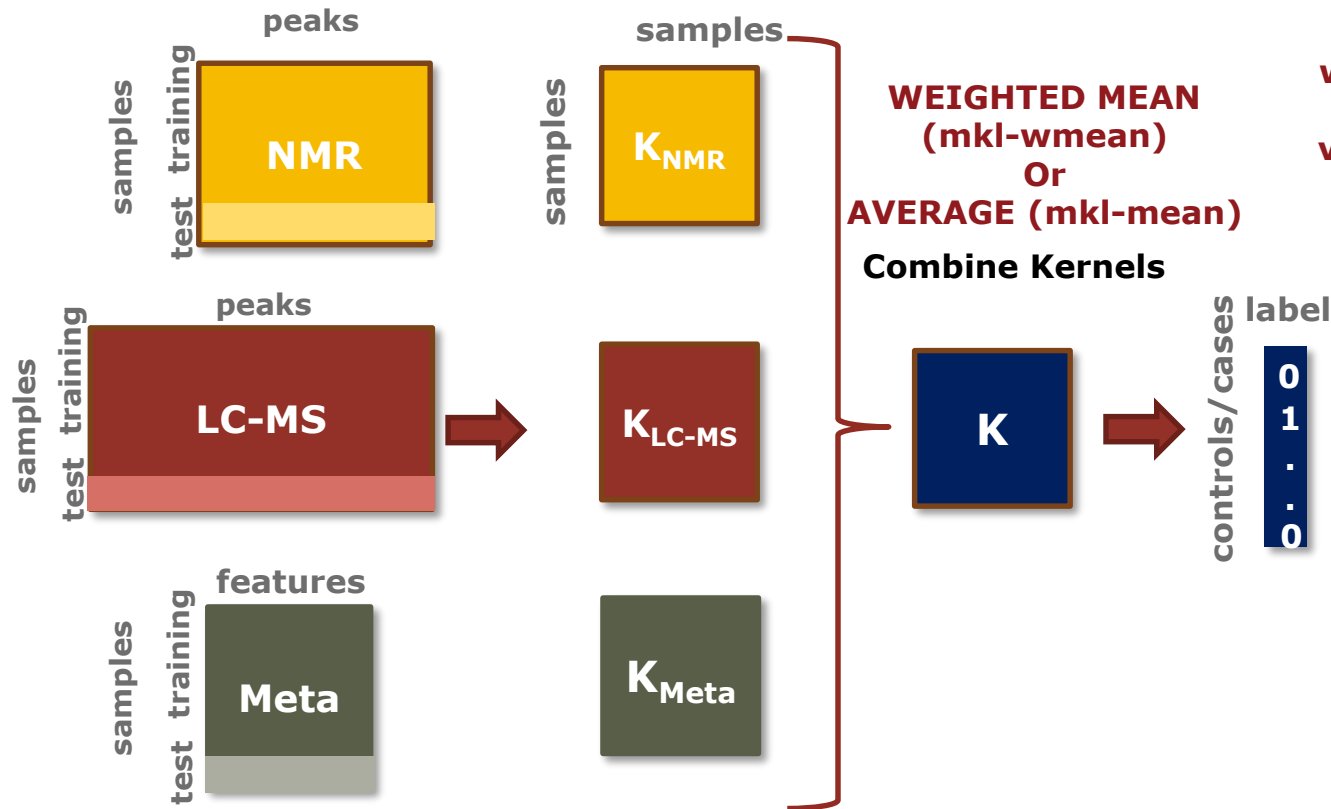


- Why not simply concatenate all views and represent each sample as one long vector of features? Due to many potential problems such as:
  - Increased risk of overfitting
  - Each data set may need different preprocessing
  - ...
- Various multi-view learning approaches [Xu et al., *arXiv:1304*, 2013]:
  - high-level approaches* such as assigning a label based on predictions of multiple classifiers
  - subspace learning-based methods* (i.e., finding latent subspaces and using those for classification)
  - multiple kernel learning*: combining kernels corresponding to different views
- Many omics studies are interested in supervised data fusion:
  - *Subspace-based approaches*: Analysis of LC-MS and GC-MS (Gas Chromatography-Mass Spectrometry) data using multi-block PLS (Partial Least Squares) [Smilde et al., 2005]; data integration in plant biology by jointly analyzing microarray and GC-MS data [Bylesjö et al., 2007]; Joint analysis of LC-MS and NMR measurements of cerebrospinal fluid samples (CSF) [Blanchet et al., 2011]
  - Multiple kernel learning: fusion of GC-MS and NMR measurements of CSF samples to study multiple sclerosis [Smolinska et al., 2012]; consensus orthogonal PLS discriminant analysis for fusion of omics data [Boccard et al., 2013]

# We use multiple kernel learning for supervised data fusion

**Multiple Kernel Learning:** Different kernels can be used as a measure of similarity for different views. Given multiple kernels, combining kernels is one possible way of combining information from multiple sources. See [Gonen and Alpaydin, 2011] for a nice survey.

**Form Kernel Matrices**  
(Linear/nonlinear kernels ??): **LINEAR**



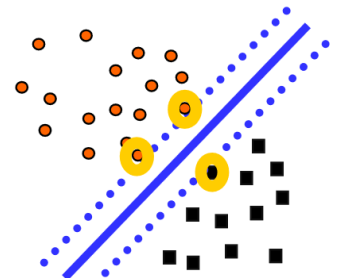
**Parameters for SVM and weights in the weighted mean are learned using cross-validation in the training data.**

**Build a classifier using Support Vector Machines**

$$D(x) = w \cdot x + b$$

$$\text{s.t. } w = \sum_{n=1}^N \alpha_n y_n x_n$$

$$b = \langle y_n - w \cdot x_n \rangle$$

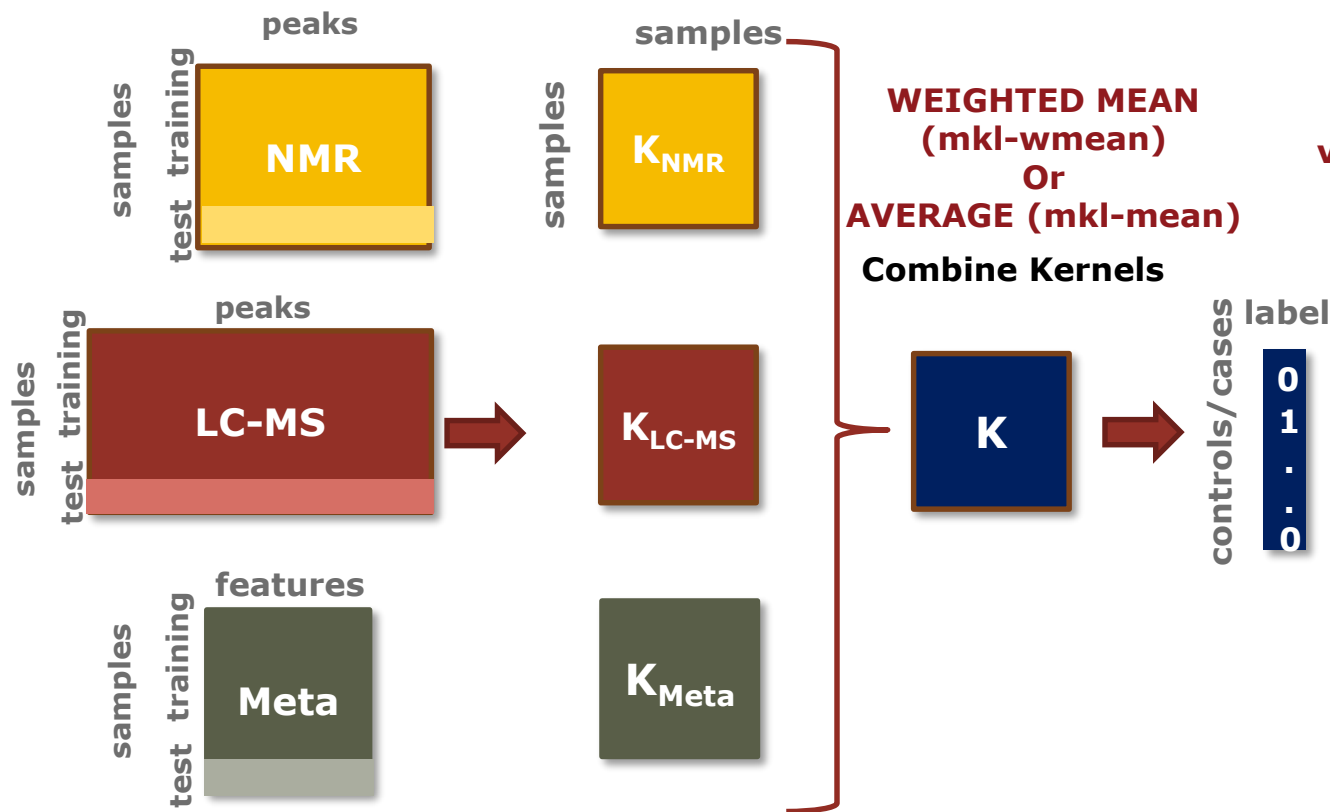


[Bennett & Campbell, 2000]

# Performance Evaluation in terms of ROC (Receiver Operating Characteristics) Curves

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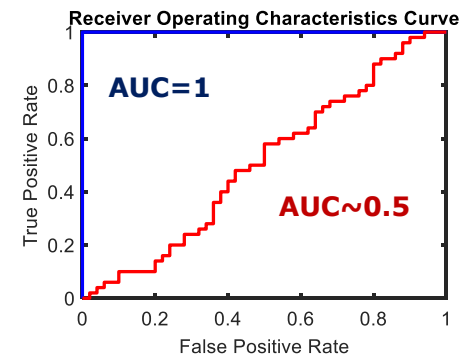
**Parameters for SVM and weights in the weighted sum are learned using cross-validation in the training data.**

**Build a classifier using Support Vector Machines**

$$f(x) = w \cdot x_{\text{test}} + b$$

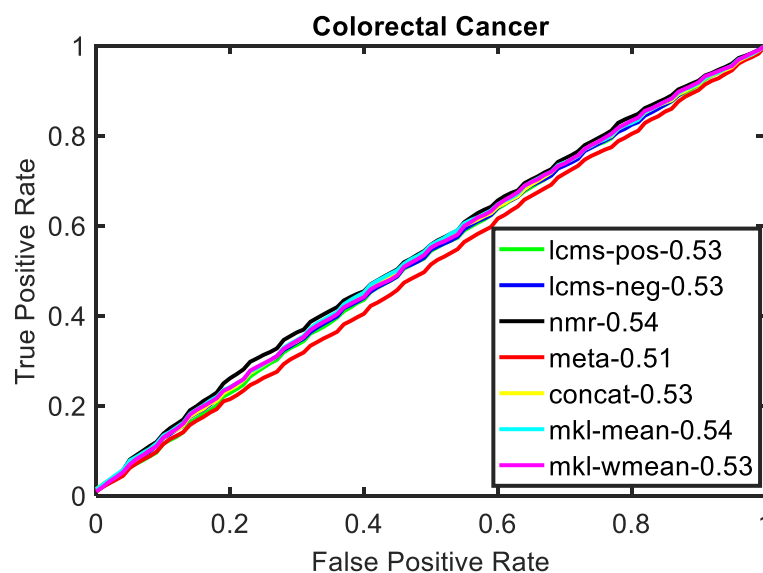
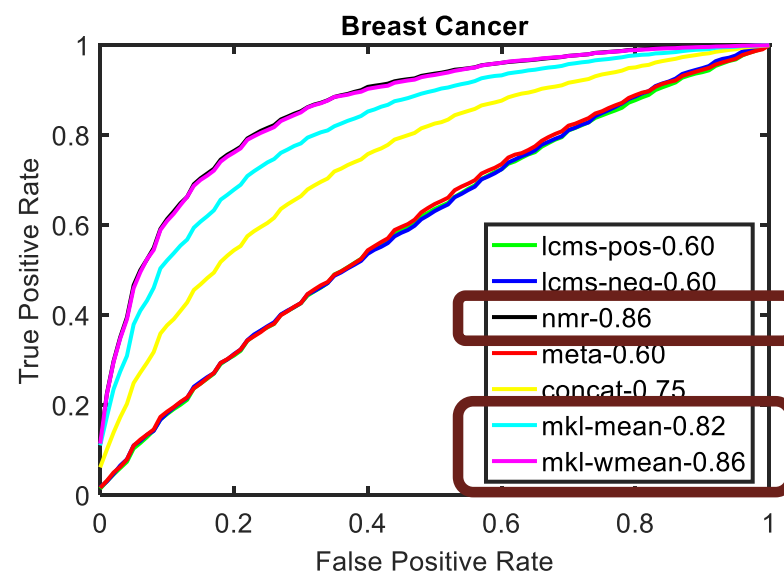
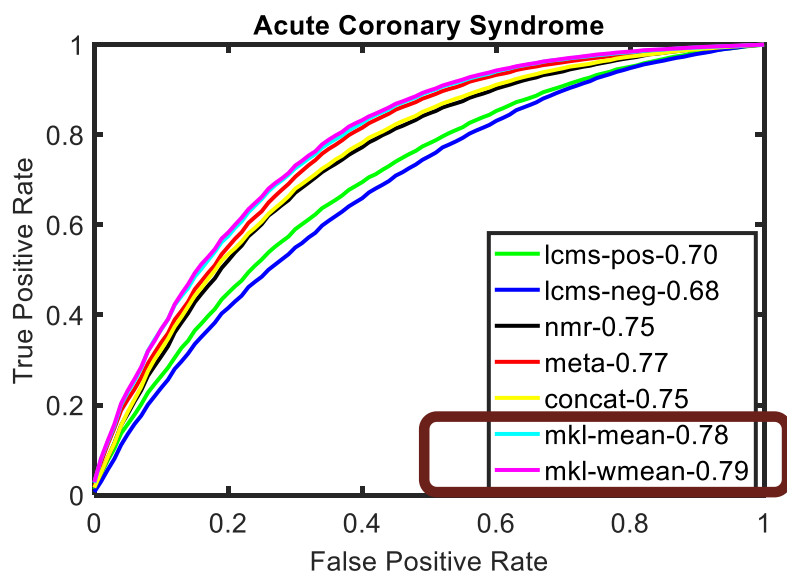
v.s.

$$y_{\text{test}}$$

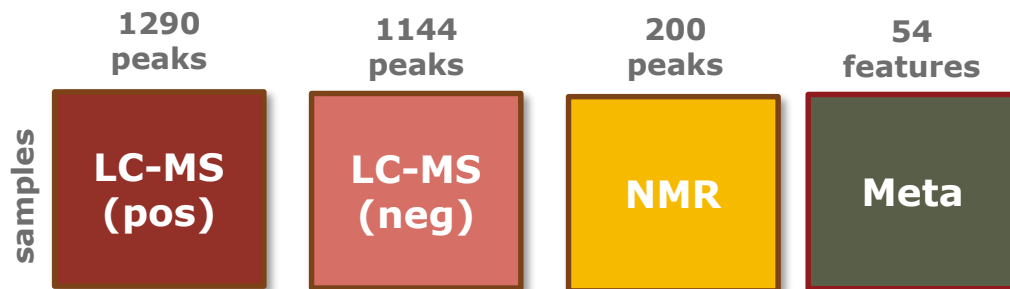




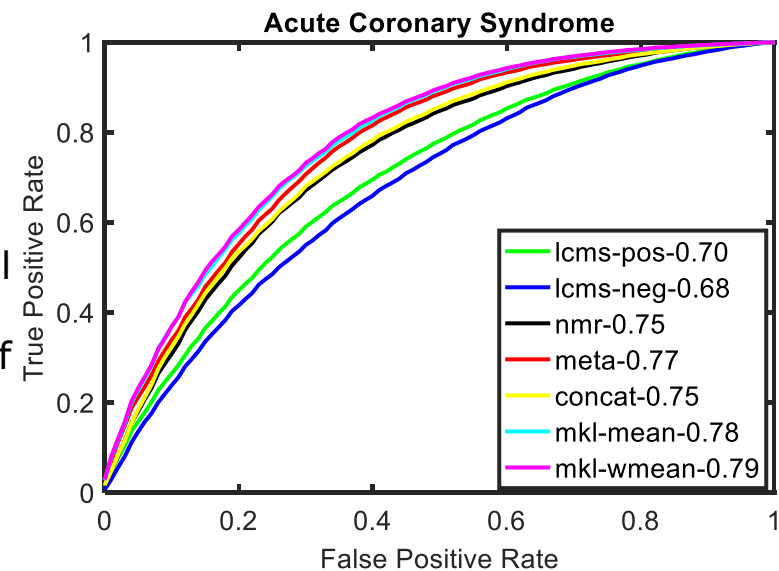
# Results Summary



# Acute Coronary Syndrome(ACS): Data fusion improves the forecasting performance for ACS!



- In total, **3376** samples (**1092** cases/ **2284** controls).
- While forming training and test sets, we take equal number of cases and controls (randomly) and use 70% of the samples as the training set and 30% of the samples as the test set, i.e.,
  - Training set: **1530** samples
  - Test set: **654** samples
- Results are based on 100 such random training – test splits.



## RESULTS:

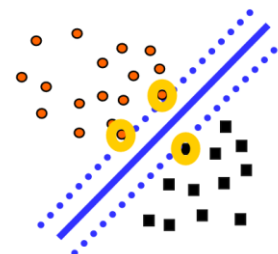
- Data fusion (using both mkl-mean & mkl-wmean) performs better than individual analysis of data sets. Note that concatenation ("concat") is not the solution!
- In mkl-wmean, weights selected by cross-validation are higher for NMR in 44% of the runs, higher for meta data in 49% of the runs, and equal for all data sets in 7% of the runs.

# ACS: Significant features in a fusion model with a performance close to the average performance (AUC=0.78)

$$D(x) = w \cdot x + b$$

$$\text{s.t. } w = \sum_{n=1}^N \alpha_n y_n x_n$$

$$b = \langle y_n - w \cdot x_n \rangle$$

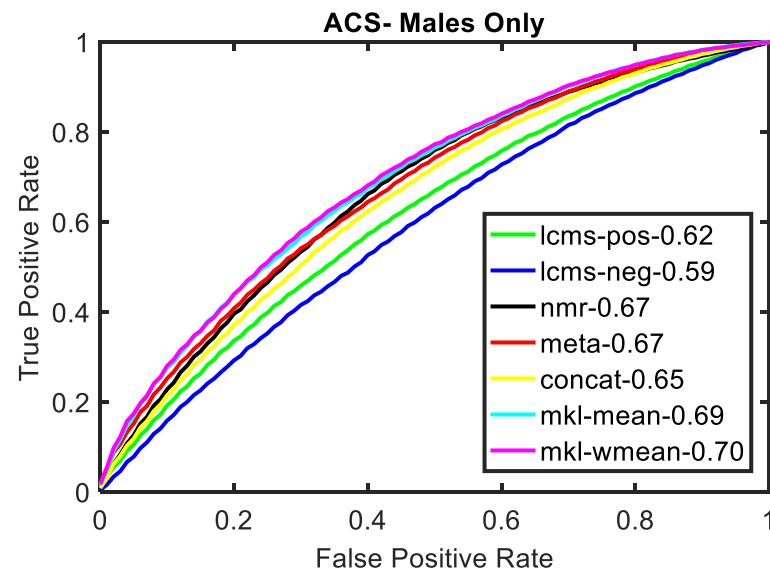
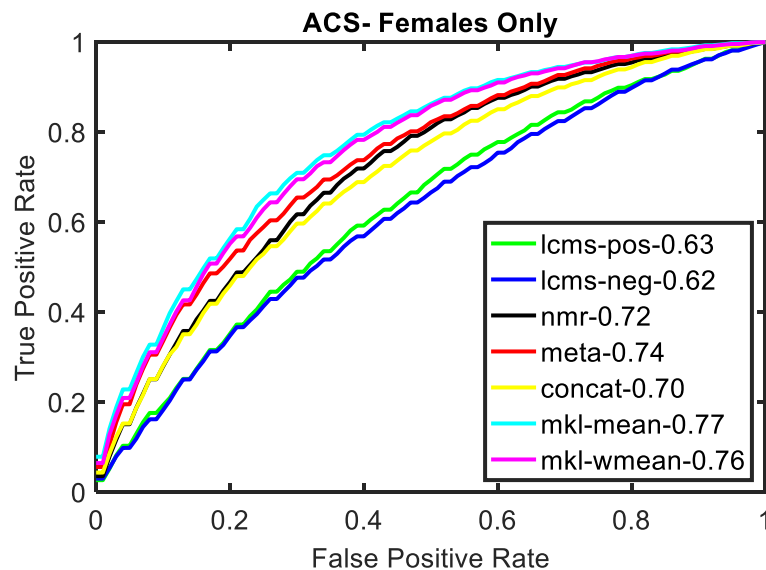


LC-MS (positive)	LC-MS (negative)	NMR	Meta
<b>Cotinine</b> ( <i>smoking</i> )	Formate cluster of unknown plasma lipids	Cholesterol	Male
Fragment of LPC(17:0) ( <i>dairy</i> )	DG(40:8)	Choline	Female
5.7719 427.2842	<b>Tetrahydrocorticosterone or Tetrahydrodeoxycortisol</b>	?	Years of smoking
<b>PE(40:6)</b>	0.49796 972.2975	?	Low-level school
4.557 417.3468	1.0378 260.0448	?	Current smoker
<b>Caffeine</b> ( <i>coffee</i> )	0.70387 111.9631	?	Never smoker
4.909 328. 2305	3.6106 725.5184	<b>Valine</b>	High-level school
4.723 594.3582	4.9296 457.225	<b>Mainly glucose and protein</b>	1 if either >35y at first birth or no children at all
0.69012 147.0294	3.0921 380.0944	?	Blood pressure
5.2717 786.507	4.7867 101.934	?	Years since quitting smoking

**Gender effect**

**Smoking**

# Acute Coronary Syndrome(ACS): Removing gender effect by looking into females and males separately!



## RESULTS:

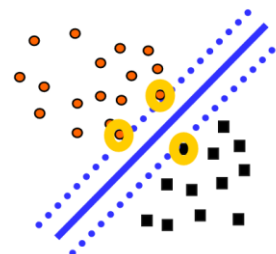
- We see a drop in performance (in females from 0.79 to 0.77, and in males from 0.79 to 0.70) so gender does indeed play a significant role.
  - Females: Training set: 362 samples, Test set: 134 samples
  - Males: Training set: 1168 samples, Test set: 500 samples
 (We can expect a decrease in the performance due to the decrease in the number of samples but still we have many samples to build the models).
- Data fusion still improves the performance in both males and females.

# ACS - Females Only: Significant features in a fusion model with a performance close to the average performance (AUC=0.77)

$$D(x) = \mathbf{w} \cdot \mathbf{x} + b$$

$$\text{s.t. } \mathbf{w} = \sum_{n=1}^N \alpha_n y_n \mathbf{x}_n$$

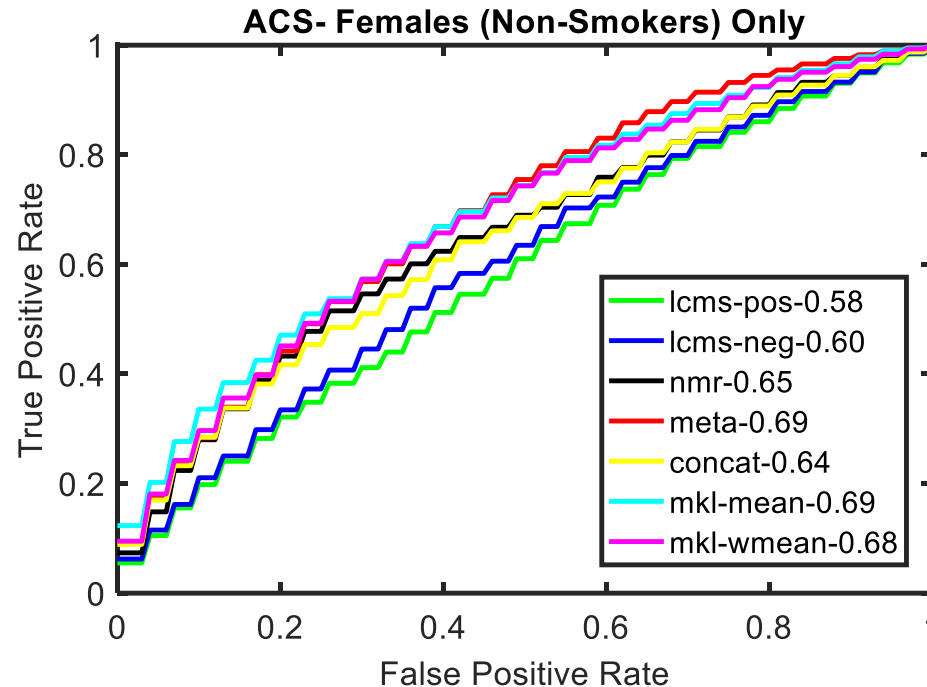
$$b = \langle y_n - \mathbf{w} \cdot \mathbf{x}_n \rangle$$



LC-MS (positive)	LC-MS (negative)	NMR	Meta
<b>Cotinine</b>	4.6767 142.9247	?	Current smoker
4.6161 277.2185	0.70361 193.1955	?	Years of smoking
5.3291 145.9565	4.2568 579.2974	?	Former smoker
3.668 472.3038	0.7048 192.3631	<b>Cholesterol</b>	Never smoker
4.4242 233.0796	4.8341 367.2635	<b>Choline</b>	High-level school
4.8958 137.06	4.8288 489.2595	?	Low-level school
<b>Testosterone</b>	0.70457 192.2054	?	Total amount of tobacco consumption (daily)
5.1136 178.9475	3.9639 445.1124	?	Years since quitting smoking
4.7973 287.1309	0.70662 192.1081	<b>Pyruvate</b>	Blood pressure, systolic
4.7477 548.3712	0.70048 111.9481	<b>Histidine</b>	Coffee (g/d)

**Smoking effect**

## ACS - Females & Non-Smokers Only: Removing the effect of smoking by looking into only former smokers and the ones who have never smoked!



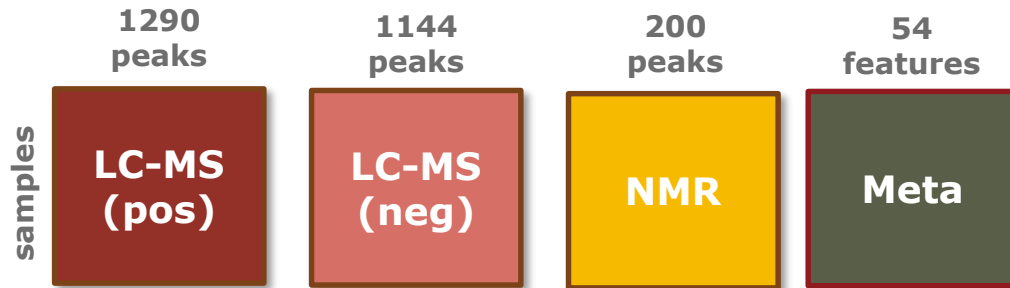
***Better than random  
but low  
performance!***

### Summary (ACS):

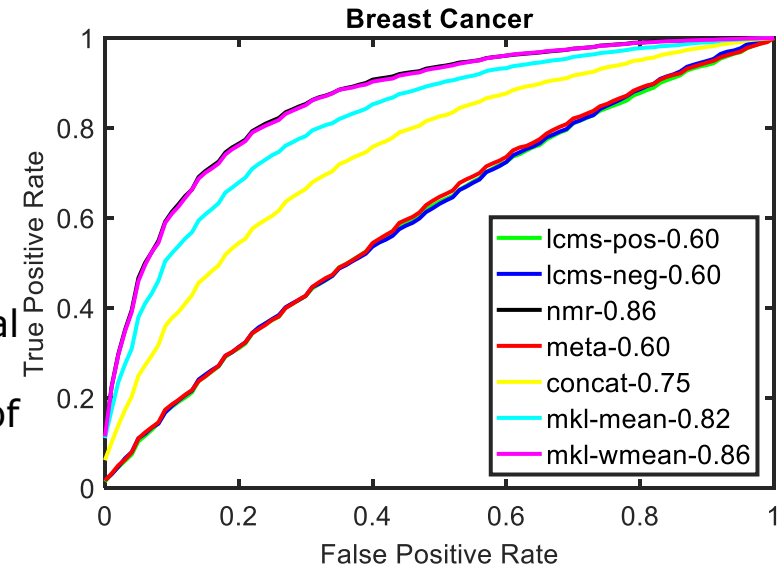
- Improved forecasting performance using supervised fusion
- Major effects are gender, smoking and cholesterol!



# Breast Cancer: Data fusion is not always a good idea!



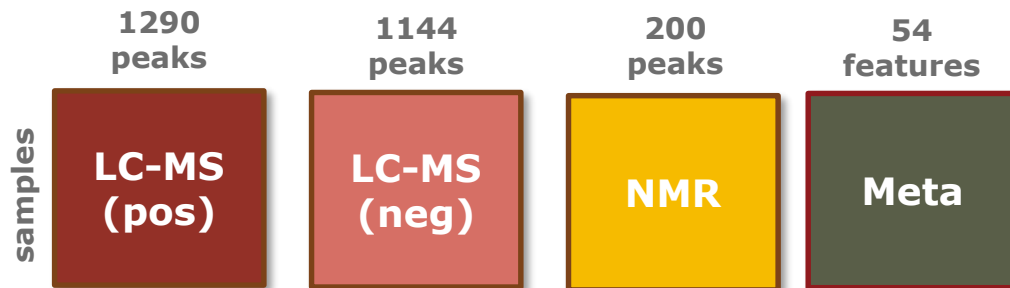
- In total, **1589** samples (**412** cases/ **1177** controls) from **females**.
- While forming training and test sets, we take equal number of cases and controls (randomly) and use 70% of the samples as the training set and 30% of the samples as the test set, i.e.,
  - Training set: **578** samples
  - Test set: **246** samples
- Results are based on 100 such random training – test splits.



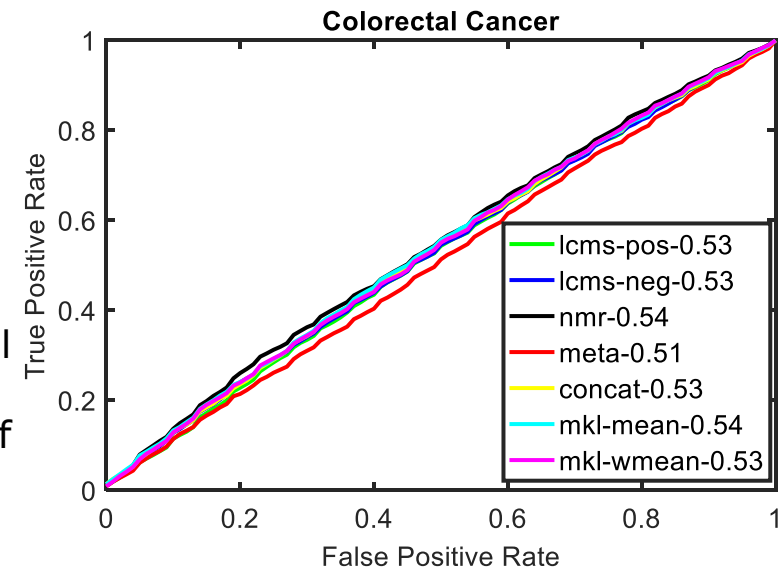
***NMR performs the best!***

**Bro et al., *Metabolomics*, 2015 achieves a similar performance using NMR and meta data.**

# Colorectal Cancer (CRC): Nothing works if the goal is to forecast CRC cases!



- In total, **3376** samples (**408** cases/ **2968** controls).
- While forming training and test sets, we take equal number of cases and controls (randomly) and use 70% of the samples as the training set and 30% of the samples as the test set, i.e.,
  - Training set: **572** samples
  - Test set: **244** samples
- Results are based on 100 such random training – test splits.

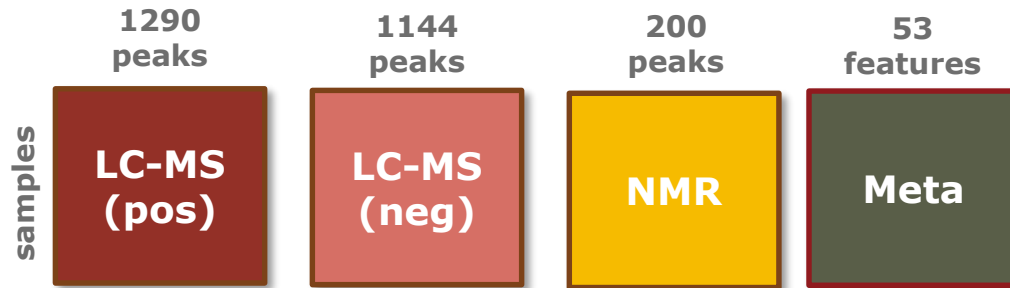


*Is it the biology, time resolution or the modeling approach???*

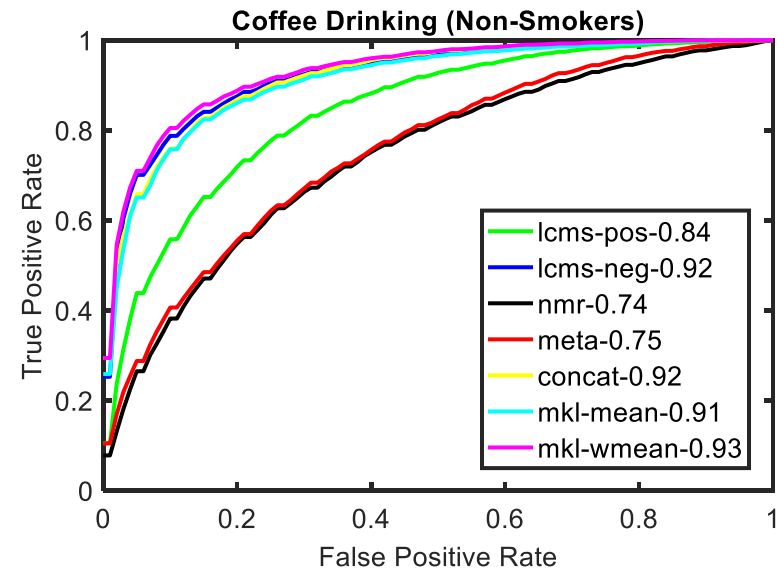


# The models reveal meaningful biomarkers!

## Case Study 1: Coffee Markers



- **Non-smokers**
- In total, **641** samples (**370** cases(coffee-drinkers)/ **271** controls (not drinking coffee)).
- While forming training and test sets, we take equal number of cases and controls (randomly) and use 70% of the samples as the training set and 30% of the samples as the test set, i.e.,
  - Training set: **380** samples
  - Test set: **162** samples
- Results are based on 100 such random training – test splits.



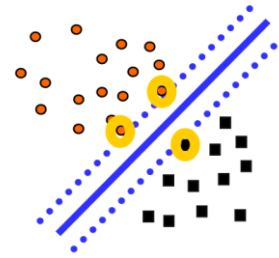
- ***Fusion using mkl-wmean improves the performance!***
- ***In 86% of the runs, mkl-wmean gives the following weights to the data sets: 0.7 (LC-MS negative), 0.1 (LC-MS positive), 0.1 (NMR), 0.1 (Meta). 11% of the runs uses only LC-MS negative mode.***

# Coffee drinking: Significant features in a fusion model with a performance close to the average performance (AUC=0.93)

$$D(x) = \mathbf{w} \cdot \mathbf{x} + b$$

$$\text{s.t. } \mathbf{w} = \sum_{n=1}^N \alpha_n y_n \mathbf{x}_n$$

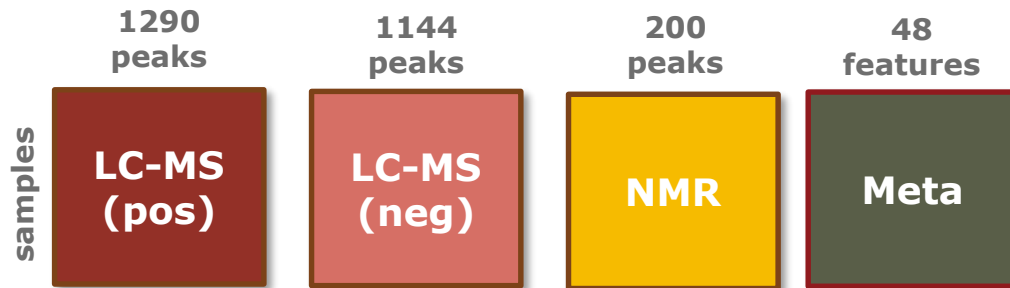
$$b = \langle y_n - \mathbf{w} \cdot \mathbf{x}_n \rangle$$



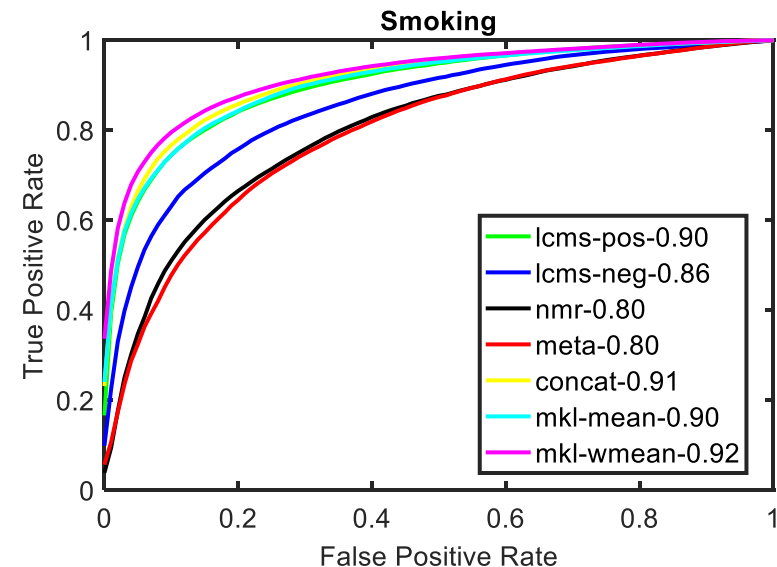
LC-MS (positive)	LC-MS (negative)	NMR	Meta
0.66518 181.0732	<b>Quinic acid</b> (coffee)	?	Rye bread[g/d]
<b>Caffeine</b> (coffee)	3.6983 495.2231 (coffee)	?	Low-level school
0.52274 138.055	3.6969 517.2054 (coffee)	<b>Creatinine</b>	High-level school
<b>1,7-dimethylxanthine Fragment</b> (coffee)	3.4666 429.1583	<b>Glucose</b>	Female
4.9097 382.2082	3.6386 413.1632	<b>Mainly glucose and protein</b>	Male
3.1213 138.0668	<b>Cafestol adduct 1</b> (coffee)	<b>Glucose</b>	Fatty dairy products (g/d)
<b>1,7-dimethylxanthine (coffee)</b>	<b>Cafestol adduct 2</b> (coffee)	?	Current user of NSAIDS
4.6052 98.98434	2.3967 195.0512	?	Never Smoker
2.3447 185.1292	<b>1 or 3 Methyluric acid</b> (coffee)	?	Former Smoker
<b>3-methylxanthine OR 7- methylxanthine</b> (coffee)	0.51941 179.0552	?	Sugars total (g/d)

# The models will also pick up the confounding variables!

## Case Study 2: Smoking Markers



- **Current smokers & never-a-smokers (former smokers excluded)**
- In total, **2466** samples (**1471** smokers/ **995** never-a-smokers).
- While forming training and test sets, we take equal number of cases and controls (randomly) and use 70% of the samples as the training set and 30% of the samples as the test set, i.e.,
  - Training set: **1394** samples
  - Test set: **596** samples
- Results are based on 100 such random training – test splits.



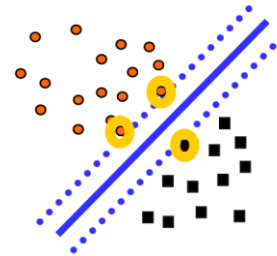
- **Data fusion using mkl-wmean performs the best!**
- **In all runs, mkl-wmean uses the following weights for the data sets: 0.7 for LC-MS positive, 0.1 for LC-MS negative mode, 0.1 for NMR and 0.1 for Meta data.**

# Smoking: Significant features in a fusion model with a performance close to the average performance (AUC=0.92)

$$D(x) = \mathbf{w} \cdot \mathbf{x} + b$$

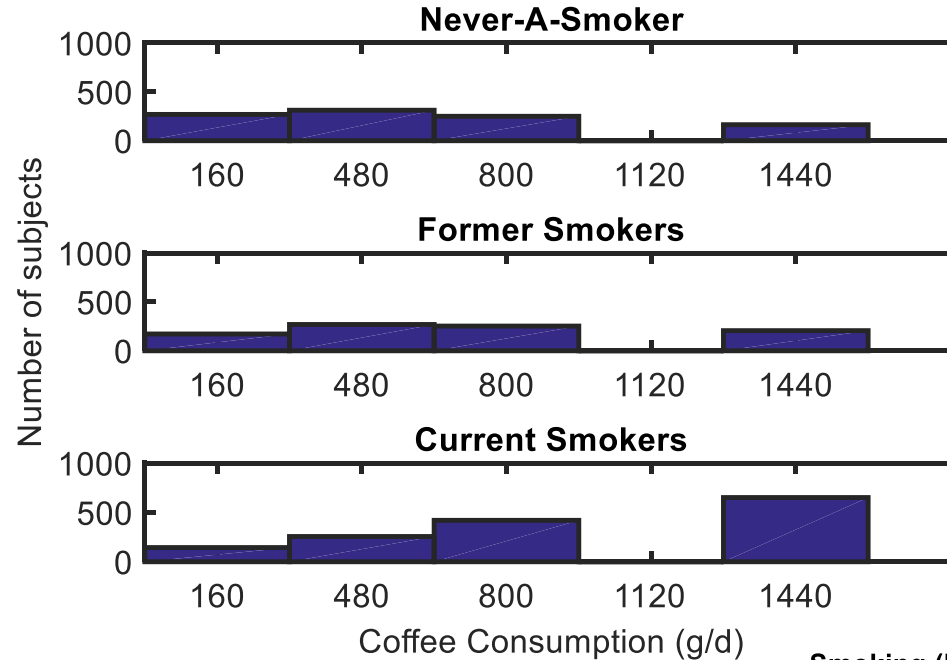
$$\text{s.t. } \mathbf{w} = \sum_{n=1}^N \alpha_n y_n \mathbf{x}_n$$

$$b = \langle y_n - \mathbf{w} \cdot \mathbf{x}_n \rangle$$

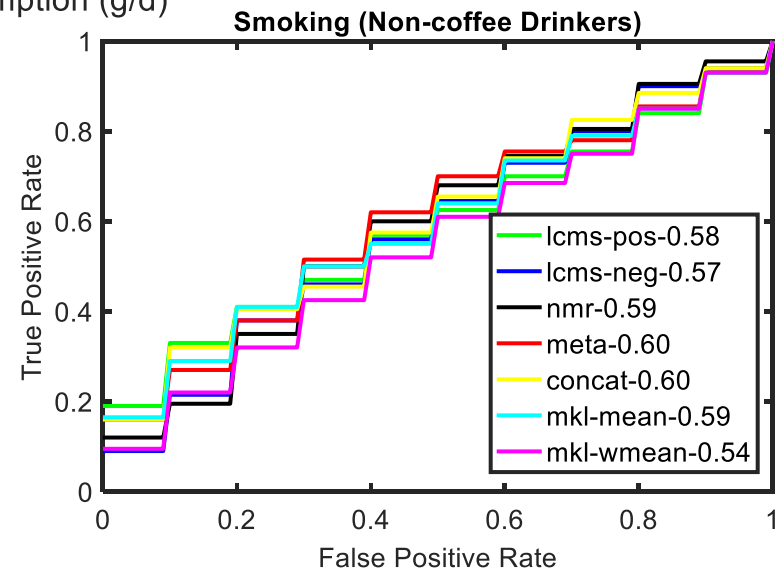


LC-MS (positive)	LC-MS (negative)	NMR	Meta
<b>Cotinine</b> ( <i>smoking</i> )	3.5214 651.3422	?	Coffee (g/d)
<b>Caffeine</b> ( <i>coffee</i> )	3.5254 199.0062	?	Low-level school
0.57949 160.1341	3.5912 201.0218	<b>Leucine and Isoleucine</b>	Medium-level school
3.1213 138.0668	0.70663 192.3785	?	Dietary fibers (g/d)
0.4542 313.0382	0.70675 391.032	?	Male
<b>3-methylxanthine OR 7-methylxanthine</b> ( <i>coffee</i> )	3.9759 435.1458	?	Female
4.7541 538.3133	4.2615 737.2553	<b>Lipid</b>	1 if either >35 y at first birth ...
0.70023 791.0996	0.70223 192.9709	<b>Choline</b>	Marine fats (n-3) in diet (g/d)
<b>Theobromine</b> ( <i>coffee</i> )	5.0276 809.0491	<b>Lipid, CH3</b>	Fruits (ex. juice) (g/d)
<b>Hesperetin 7-o- a-d-glucuronide</b>	0.70775 192.9034	?	Carbohydrate (g/d)

## Smoking: Smokers drink more coffee!

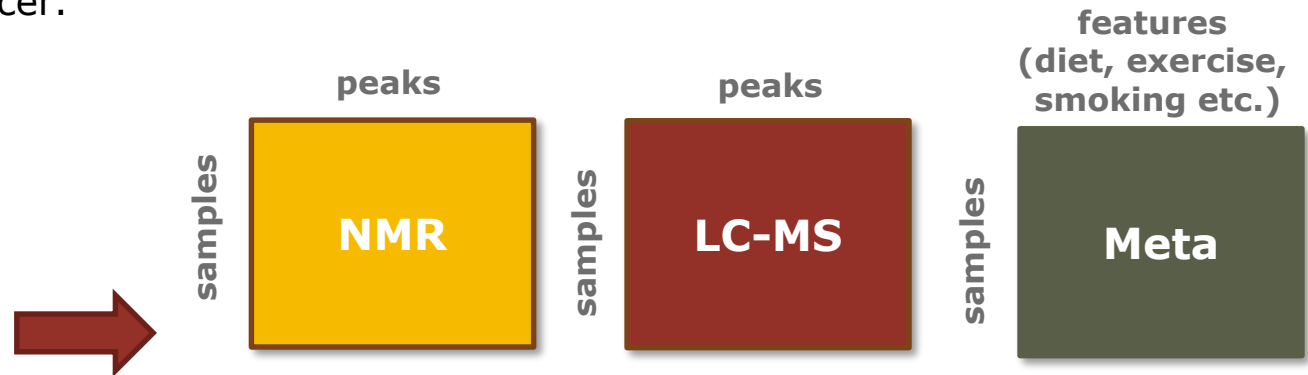


In order to eliminate the coffee effect, if we only take the subjects who do not drink coffee, we are left with very few samples and cannot build good models (64 never-a-smoker & 35 smokers).



# Revisiting: Joint analysis of measurements from multiple platforms has the potential to enhance biomarker discovery!

**Metabolomics:** The goal is to detect a wide range of chemical substances in biological fluids, e.g., blood, and to identify the chemicals related to certain conditions such as food intake and various diseases, e.g., cancer.



**1. Given these data sets, can we forecast whether people will have certain diseases in near future?**

**Yes!**

**2. Does data fusion improve our forecasting performance?**

**Depends on the disease!**

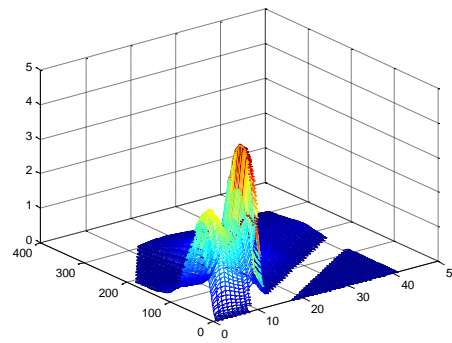
**3. Can we capture biomarkers? Are we confident with the biomarkers?**

**We can capture biomarkers but we should be aware of the confounding effects!**

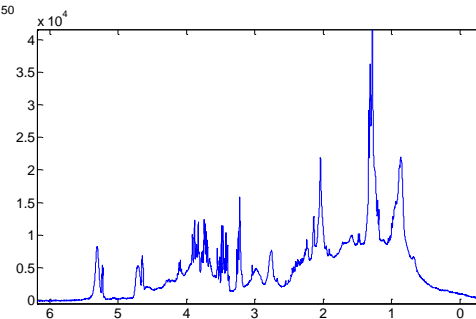
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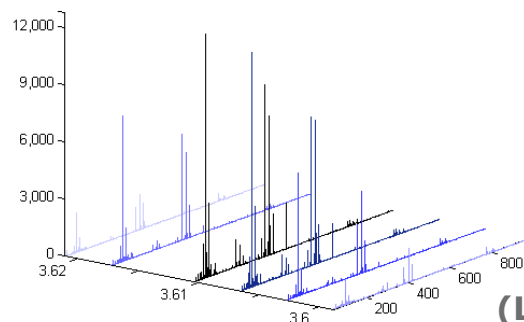
Possible to measure  
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**EEM (Fluorescence Spectroscopy)**



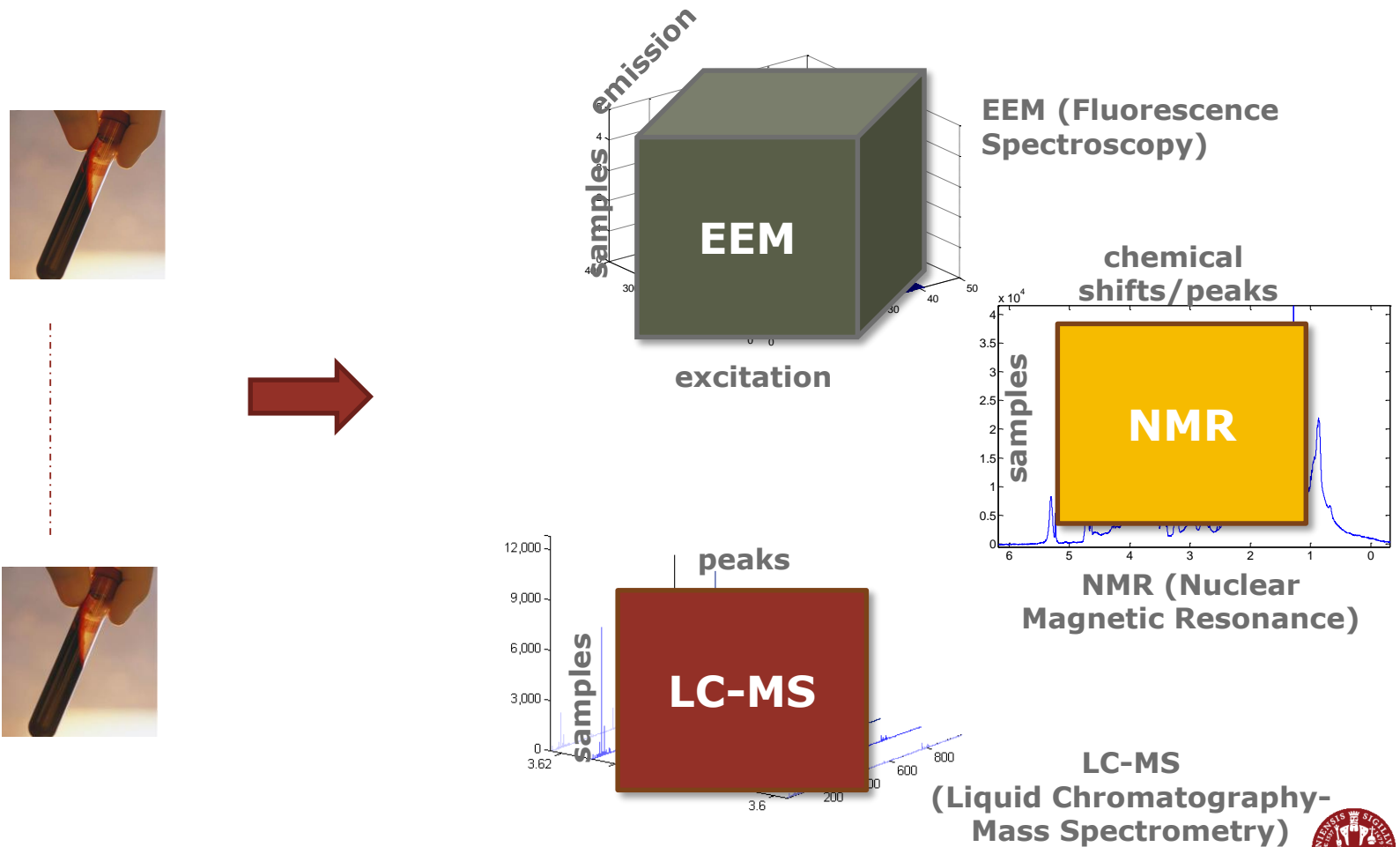
**NMR (Nuclear Magnetic Resonance)**



**LC-MS  
(Liquid Chromatography-  
Mass Spectrometry)**

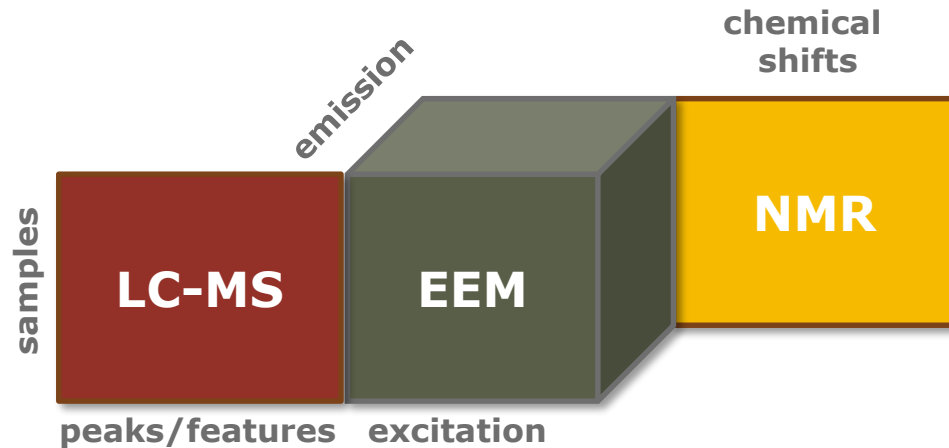


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*How can we jointly analyze these coupled matrices and higher-order tensors to enhance knowledge discovery?*



# Unsupervised Data Fusion using Coupled Matrix and Tensor Factorizations (CMTF)

Joint analysis of heterogeneous data from multiple sources can be formulated as a coupled matrix and tensor factorization problem. In CMTF, higher-order tensors and matrices are simultaneously factorized by fitting a CP model to higher-order tensors and factorizing matrices in a coupled manner.

## Matrix Factorization:

$$Y \approx \begin{bmatrix} a_1 \\ \vdots \\ a_R \end{bmatrix} \begin{bmatrix} d_1 & \dots & d_R \end{bmatrix}$$

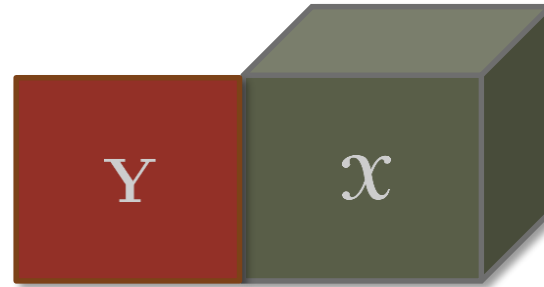
$$Y \approx \sum_{r=1}^R a_r d_r^T$$

$$\approx AD^T$$

$$A \in \mathbb{R}^{I \times R} = [a_1 \ \dots \ a_R]$$

$$D \in \mathbb{R}^{M \times R} = [d_1 \ \dots \ d_R]$$

$$Y \approx AD^T \quad \mathcal{X} \approx [A, B, C]$$



## Tensor Factorization: CANDECOMP/PARAFAC(CP)

[Hitchcock, 1927; Harshman, 1970; Carroll & Chang, 1970]

$$\mathcal{X} \approx \begin{bmatrix} a_1 \\ \vdots \\ a_R \end{bmatrix} \begin{bmatrix} b_1 & \dots & b_R \end{bmatrix} \begin{bmatrix} c_1 & \dots & c_R \end{bmatrix}$$

$$\mathcal{X} \approx \sum_{r=1}^R a_r \circ b_r \circ c_r$$

$$\approx [A, B, C]$$

$$A \in \mathbb{R}^{I \times R} = [a_1 \ \dots \ a_R]$$

$$B \in \mathbb{R}^{J \times R} = [b_1 \ \dots \ b_R]$$

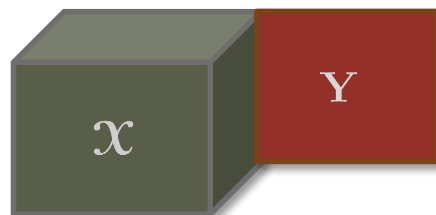
$$C \in \mathbb{R}^{K \times R} = [c_1 \ \dots \ c_R]$$

The problem can be formulated as:

$$\min_{A, B, C, D} \| \mathcal{X} - [A, B, C] \|^2 + \| Y - AD^T \|^2$$



# Data Fusion based on Coupled Tensor Factorizations



$$\min_{A,B,C,D} \| \mathcal{X} - \llbracket A, B, C \rrbracket \|^2 + \| Y - AD^T \|^2$$

- **Psychometrics:** Linked-mode PARAFAC [Harshman and Lundy, 1984]
- **Chemometrics:** Multi-way Multi-block component models [Smilde et al., 2000]
- **Bioinformatics:** Coupled analysis of in vitro and histology tissue samples [Acar et al., 2012]
- **Signal Processing:** Joint analysis of a covariance matrix and a cumulant tensor [De Lathauwer and Vandewalle, 2004; Comon, 2004]; Generalized Coupled Tensor Factorizations [Yilmaz et al., 2011]; Structured Data Fusion [Sorber et al., 2015]
- **Data Mining:** Multi-way Clustering [Banerjee et al., 2007]; Community detection [Lin et al., 2009]; Missing value estimation [Zheng et al., 2010]; All-at-once optimization for CMTF [Acar et al., 2011]; Link prediction [Ermis et al., 2012]; Scalable CMTF approaches (sampling-based [Papalexakis et al., 2014], distributed stochastic gradient running on MapReduce [Beutel et al., 2014], distributed ALS running on MapReduce [Jeon et al., 2016])

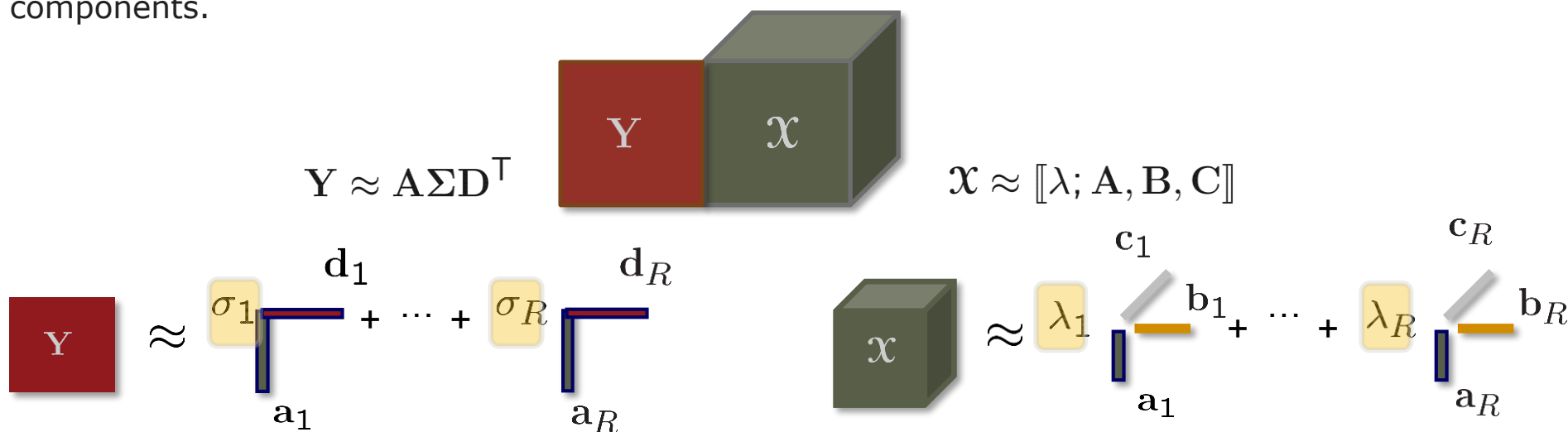
## Models identifying shared/unshared factors:

- Structure-revealing data fusion models [Acar et al., 2013; Acar et al., 2014; Acar et al., 2015]
- Mining labelled tensors by discovering common and discriminative subspaces [Lie et al., 2013]
- Joint decompositions with flexible couplings [Farias et al., 2015; Rivet et al., 2015]

# Our Approach: Structure-Revealing CMTF

[Acar et al., *BMC Bioinformatics*, 2014]

We reformulate the coupled matrix and tensor factorization problem by having factor matrices with unit norm columns and explicitly representing the weights of rank-one components in the formulation. Through modeling constraints/penalties, we let the model identify shared/unshared components.



## Structure-revealing model:

$$\min_{A, B, C, D, \Sigma, \lambda} \|X - [\lambda; A, B, C]\|^2 + \|Y - A \Sigma D^T\|^2 + \beta \|\lambda\|_1 + \beta \|\sigma\|_1$$

s.t.  $\|a_r\|_2 = \|b_r\|_2 = \|c_r\|_2 = \|d_r\|_2 = 1$ , for  $r = 1, \dots, R$

**l1-norm**

$$\|x\|_1 = \sum |x_i|$$

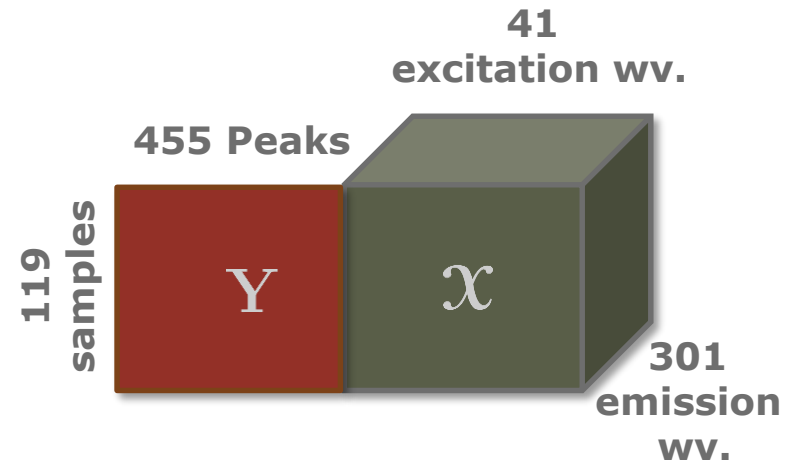
## Original CMTF

$$\min_{A, B, C, D} \|X - [A, B, C]\|^2 + \|Y - A D^T\|^2$$

# Application: Cancer Metabolomics

[Acar et al., *IEEE EMBC*, 2013]

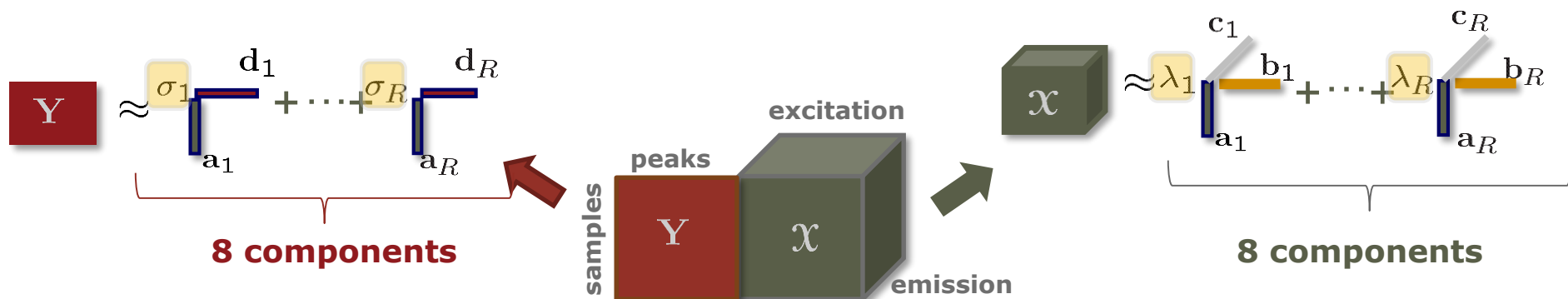
- Plasma samples measured using fluorescence spectroscopy and  $^1\text{H}$  NMR.
- 119 samples (61 Female/58 Male)
  - **cancer:** 55 samples from verified colorectal cancer (CRC)
  - **control:** 64 samples with other nonmalignant findings
- **NMR** data is converted to a set of peaks.
- **Fluorescence** measurements: Samples measured with excitation wavelengths from 250 to 450 with 5 nm increment, and emission wavelengths from 300 to 600 with 1 nm increment.



**Goal:** *We want to jointly analyze these data sets and identify shared and unshared components, and if there are any components related to CRC.*



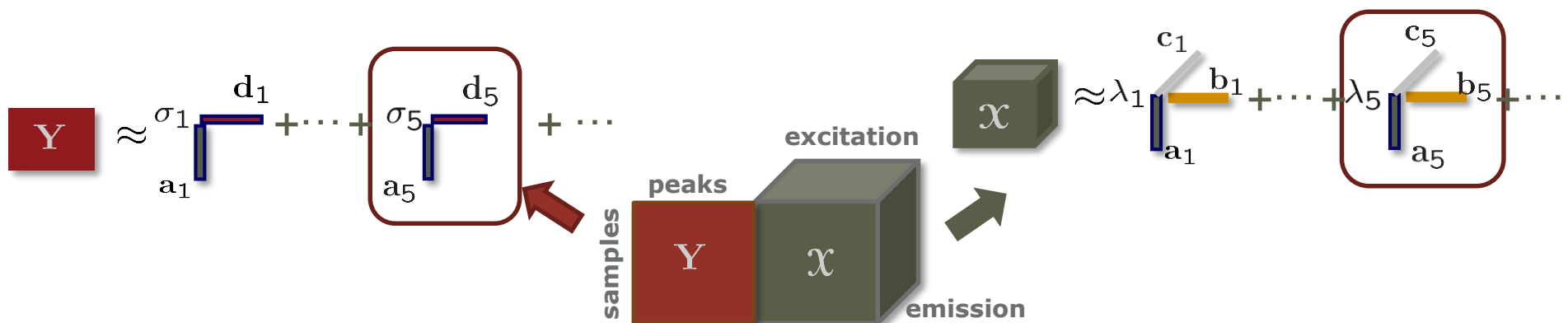
# Structure-Revealing CMTF captures shared/unshared components!



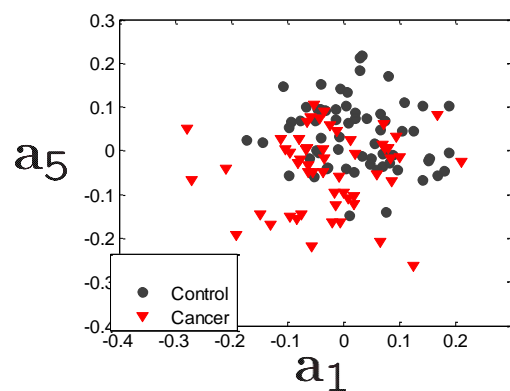
$\sigma_r$	$\lambda_r$
0.14	0.82
0.20	0.72
0.35	0.30
0.14	0.39
0.42	0.10
0.59	0.06
0.46	0.09
0.39	0.00

Only in NMR

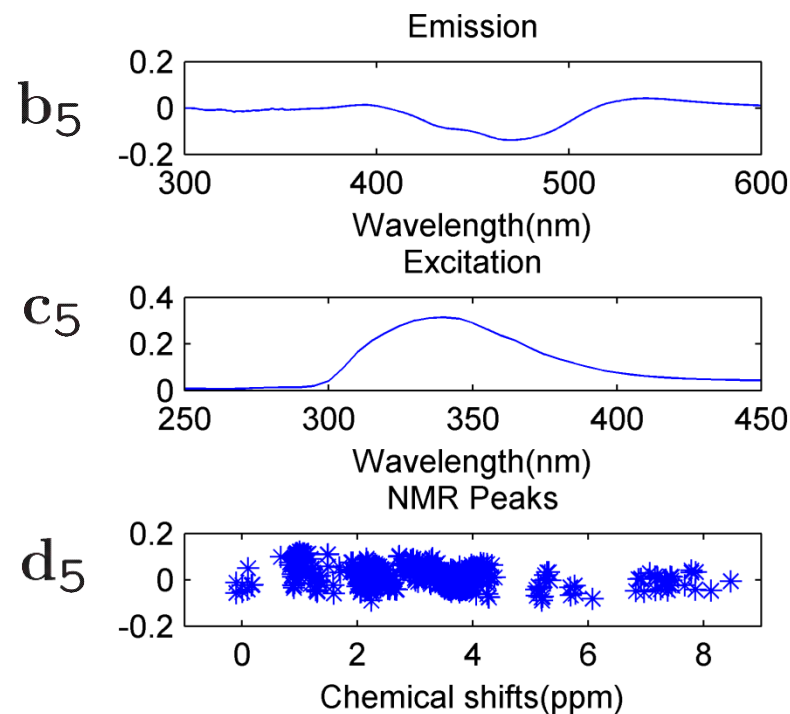
# Cancer-related component:



$\sigma_r$	$\lambda_r$
0.14	0.82
0.20	0.72
0.35	0.30
0.14	0.39
0.42	0.10
0.59	0.06
0.46	0.09
0.39	0.00



**Accuracy: 71%**  
**Sensitivity: 64%**  
**Specificity: 78%**



# Summary

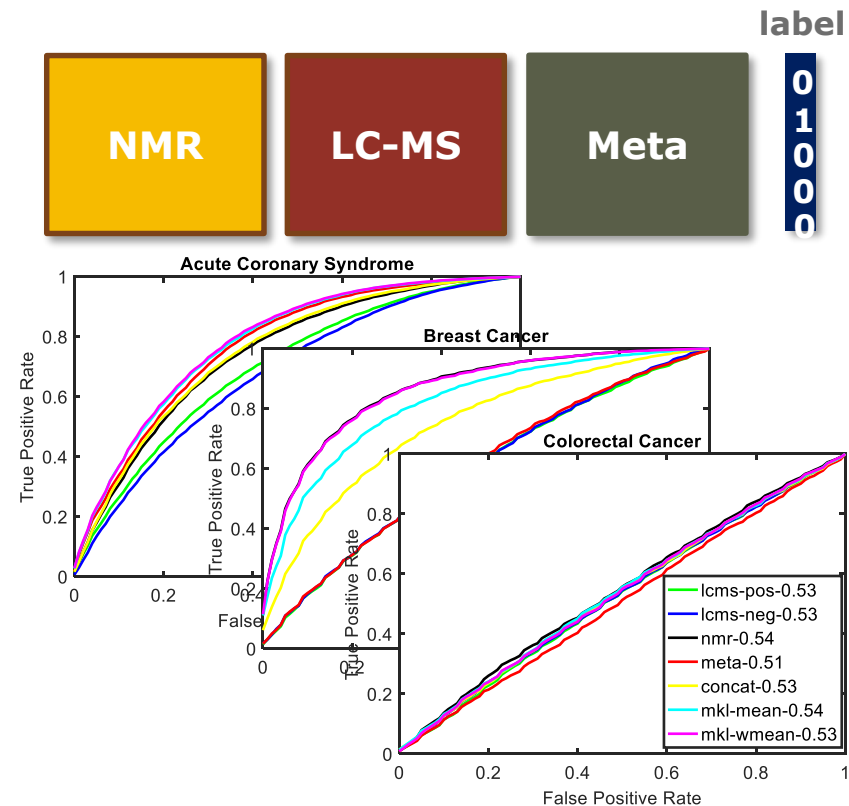
**Goal:** To forecast Acute Coronary Syndrome, Breast Cancer and Colorectal Cancer using measurements from multiple platforms and the meta data.

**Approach:** Supervised data fusion using multiple kernel learning

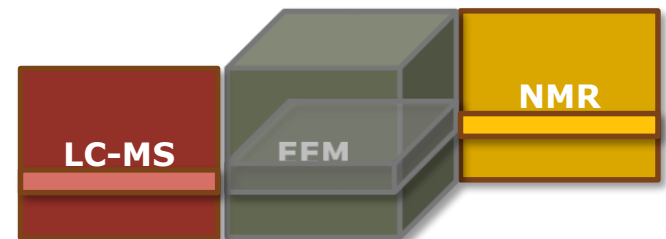
- Using linear kernels (no improvements in performance yet using nonlinear kernels)
- Identifying significant features

## Results:

- ACS: Data fusion improves the forecasting performance.
- Breast Cancer: Fusion degrades the forecasting performance.
- CRC: Neither the individual data sets nor their fusion can forecast CRC cases.
- Validation of the models by capturing known biomarkers (e.g., for coffee)
- Limitations of the models due to the confounding effects (e.g., for smoking)



**Joint analysis of data sets in the form of matrices and higher-order tensors in cancer metabolomics**





# Thank you!



## Structure-revealing data fusion model

E. Acar, R. Bro, and A. K. Smilde, Data Fusion in Metabolomics using Coupled Matrix and Tensor Factorizations, *Proceedings of the IEEE*, 103: 1602-1620, 2015.

E. Acar, E. E. Papalexakis, G. Gurdeniz, M. A. Rasmussen, A. J. Lawaetz, M. Nilsson, and R. Bro, Structure Revealing Data Fusion, *BMC Bioinformatics*, 15: 239, 2014.

E. Acar, M. Nilsson, and M. Saunders, A Flexible Modeling Framework for Coupled Matrix and Tensor Factorizations, *EUSIPCO*, pp. 111-115, 2014.

E. Acar, A. J. Lawaetz, M. A. Rasmussen, and R. Bro, Structure Revealing Data Fusion Model with Applications in Metabolomics, *IEEE EMBC*, pp. 6023 - 6026, 2013.

**Evrin Acar**

<http://www.models.life.ku.dk/~acare/>

**JODA: Joint Data Analysis for Enhanced Knowledge Discovery**

<http://www.models.life.ku.dk/joda>